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# Behaviour of transdanubian clay under unloading and reloading

## Comportement des transdanubiennes sols argileuses pendant chargement et déchargement

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### ABSTRACT

In recent years, in the field of geotechnical design, software based on FEM has come to the front. Advanced computer programs make it possible to use more developed soil models besides the most current elastic-plastic Mohr-Coulomb model. By using these computer programs, nonlinear behaviour of the soil can be followed better, even in the case of more complicated load events. Among the constitutive models incorporated in the commercial software the Hardening Soil Model (HS) and Soft Soil Model (SS) are the most promising ones. Observations and experience gained in tunnel construction, deep open excavation or preloaded embankment prove that with these soil models reality can be followed more accurately, especially in cases where unloading and reloading are present.

In order to produce the software input parameters, in case of more complicated soil model, more demanding laboratory tests are needed. In case of HS model one of the basic demands is to determine the power for stress-level dependency of stiffness ( $m$ ), tangent stiffness for primary oedometer loading ( $E_{\text{oed}}^{\text{ref}}$ ) and unloading/reloading stiffness ( $E_{\text{ur}}^{\text{ref}}$ ).

The paper focuses on the behaviour of transdanubian clay common in Hungary. Sampling, laboratory investigations and evaluation aimed to determine the input parameters for the HS are described. Results based on a number of oedometric tests accomplished with unloading and reloading proved to be adequate for the computational purposes.

### RÉSUMÉ

Dans ces dernières années, des logiciels monté sur la méthode des éléments finis se mettre en avant dans le domaine du projet de géotechnique. Ces nouvelles logiciels permettent d'utiliser diverses modèles avancées à côté de la modèle plastique-élastique (Mohr-Coulomb) qui est la plus courante. En utilisant ces nouvelles modèles, on peut suivre mieux la comportement de la sol en cas des chargement compliqués. Celles la modèle durcissement (Hardening Soil Model-HS) et la modèle sol spongieux (Soft Soil Model-SS) qui sont les plus prometteuses. En juger par l'expérience des mesures, il est possible de suivre la réalité plus précisément, particulièrement dans les cas de déchargement et/ou réchargement, par exemple des tunnels, des fouilles de travaux ou des remblais préchargés.

Pour identifier les paramètres d'inputs d'une modèle de la sol plus compliquée, on a besoin des test de laboratoire plus détaillé. Définir du changement d'indice d'une puissance de la coefficient de compression typique de la première chargement et la définition des coefficient relatifs pendant déchargement et rechargement - ces sont des exigences essentielles ( $m$ ,  $E_{\text{oed}}^{\text{ref}}$ ,  $E_{\text{ur}}^{\text{ref}}$ ).

On a fait des recherches sur le comportement des sols argileuses hongroises, utilisent les échantillons effectué sur le Sud de la Transdanubia. L'objectif de cette investigation scientifique a été la détermination des paramètres d'inputs de la modèle HS dans le cas de la sol argileuse transdanubienne. Les résultats se basent sur les nombreuses test oedométrique, accomplissent réchargement/déchargement.

Keywords : nonlinear constitutive model, Plaxis, Hardening Soil Model, clay

## 1 INTRODUCTION

In civil engineering lately we have several projects where unloading and reloading are present. The typical case is creating a deep excavation in an urban area or applying preload to an embankment. Movements induced by consecutive excavations demand more accurate calculation and analysis of soil-structure interaction especially in urban areas. In such cases the strains and displacements cannot be described accurately by the conventional constitutive model: the elasto-plastic model with Mohr-Coulomb failure criteria. Excavation and reloading can be analyzed only by a constitutive model capable of describing nonlinear behavior and hardening process. Advanced programs like PLAXIS now make it possible to use more complex soil models. The two most promising new models are: the Hardening Soil Model (HS); and the Soft Soil Model (SS). Observations and experience gained in tunnel construction, deep excavations, and preloaded embankments show that these soil models more accurately describe field behavior. This is especially true where there are complex loading and unloading sequences in construction.

Geotechnicians using these computational facilities often face the problem of having inadequate or inaccurate data for preliminary geotechnical estimations or suggestions for structural design. To overcome this difficulty the laboratory at Széchenyi István University has performed approximately two hundred oedometer tests using unloading and reloading during the last few years. We have analyzed the test results and established correlations with the computational model parameters. The aim of this research was to determine reliable relationships to substitute or estimate missing data and serve as a design aid during the preliminary phase of a project.

## 2 INVESTIGATED SOIL PROPERTIES

Table 1. shows the main parameters of the tests. The plasticity index ranges between 9 % and 60 % with an average value of 21 %. The consistency index is between 0,5 and 1,6, the average value is 1.0. The average value of the oedometer modulus due to primary compression is 12 MPa, and the average elastic unloading/reloading modulus is 47 MPa. Note that the unloading/reloading is about four times the primary

compression. This is in line with recommendations in the Plaxis manual which states that the quotient should be between three and five. The collected data have been evaluated statistically and correlations have been evaluated, and these results are presented below.

The samples originated from the southern part of Hungary. The points are above the A-line and diverge from the A-line with increasing liquid limit values (Figure 1). The equation of the best-fit line is  $I_p=0,85 \cdot (w_L-18,2)$  with a correlation coefficient  $r = 0,95$ . The tested samples plot are above the A-line, so they are mainly medium and high plasticity clay but with some silt too.

Figure 2. shows the relationship between water content and consistency index. The linear correlation is described by the equation  $I_c=1,9-0,04 \cdot w$ , with a correlation coefficient  $r=0,7$ .

### 3 PARAMETERS OF HARDENING SOIL MODEL

The Hardening Soil model (HS) is an advanced model for simulating the behavior of different types of soil, both soft and hard. A basic feature of the present HS model is the stress dependency of soil stiffness. The HS model uses moduli both from oedometer tests and from triaxial tests. Oedometer test results demonstrate the dependence of stiffness on confining stress. The increase of the oedometric modulus depends on the mean hardening stress. This is described by the equation

$$E_{oed} = E_{oed}^{ref} \cdot \left( \frac{c \cdot ctg\phi - \sigma'_1}{c \cdot ctg\phi + p^{ref}} \right)^m \quad (1)$$

where the  $E_{oed}^{ref}$  is the reference oedometer modulus, and the strength and stress parameters are raised to the power  $m$ . The reference pressure,  $p^{ref}$  is typically 100 kPa. Under triaxial conditions, the parameter  $E_{50}$  is the confining stress dependent stiffness modulus for primary loading and is given by the equation

$$E_{50} = E_{50}^{ref} \cdot \left( \frac{c \cdot ctg\phi - \sigma'_3}{c \cdot ctg\phi + p^{ref}} \right)^m \quad (2)$$

where  $E_{50}^{ref}$  is a reference stiffness modulus corresponding to the reference confining pressure  $p^{ref}$ . For unloading and reloading stress paths, another stress-dependent stiffness modulus is used (figure 3) :

$$E_{ur} = E_{ur}^{ref} \cdot \left( \frac{c \cdot ctg\phi - \sigma'_3}{c \cdot ctg\phi + p^{ref}} \right)^m \quad (3)$$

where  $E_{ur}^{ref}$  is the reference Young's modulus for unloading and reloading, corresponding to the reference pressure  $p^{ref}$ .

Table 1. Properties of the investigated soil

parameter	minimum value	maximum value	average value	
w	%	10,0	35,0	22,5
$I_p$	%	9,0	59,9	20,9
$I_c$	-	0,5	1,6	1,0
$E_{oed}$	MPa	3,7	40,4	12,3
$E_{ur}$	MPa	8,6	125,6	46,6
A	-	0,007	0,118	0,032
B	-	0,22	0,92	0,57
m	-	0,08	0,78	0,43

Application of the HS model requires the user to have known  $m$ ,  $E_{oed}^{ref}$  modulus and  $E_{ur}^{ref}$  modulus.

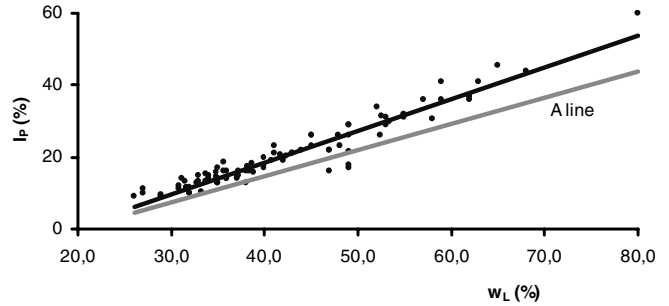


Figure 1. Correlation of  $I_p - w_L$

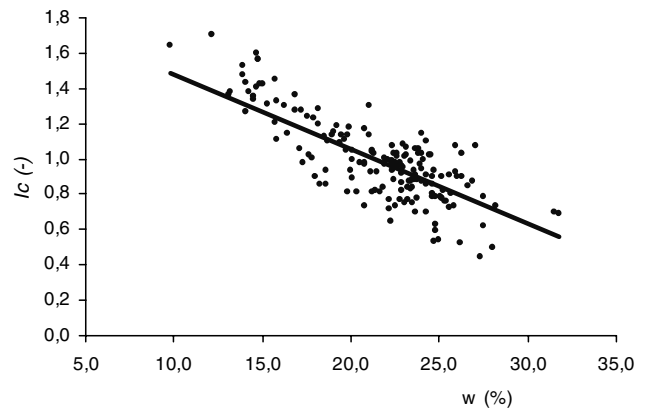


Figure 2. Best-fit linear regression between consistency index,  $I_c$  and water content,  $w$

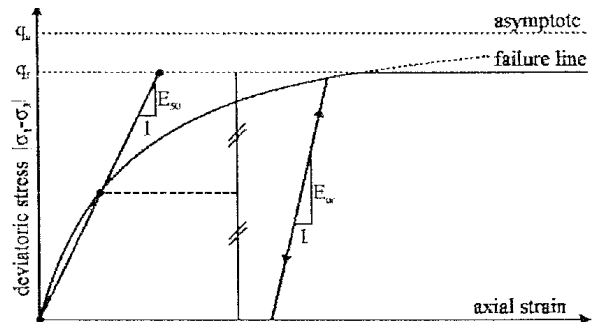


Figure 3. Deviatoric stress vs. axial strain showing  $E_{50}$  and  $E_{ur}$

In order to determine the modulus input parameter, we model the stress-strain behavior as a power curve (as suggested by Janbu) :

$$\epsilon_z = A \left( \frac{\sigma_z}{p} \right)^B \quad (4)$$

where  $\epsilon_z$  – the vertical specific strain,  $\sigma_z$  - the vertical stress,  $A$  – scale factor relating stress and strain,  $B$  – power factor relating stress and strain,  $p=100$  kPa. With this formula we get the same shape as it is in the HS model. By taking the derivative of the

$$E_s = \frac{p}{A \cdot B} \cdot \left( \frac{\sigma_z}{p} \right)^{1-B} \quad (5)$$

equation, we can formulate the oedometric tangent modulus as a function of  $\sigma_z$ :

Figure 4. shows the relation between A and B. The correlation can be described by the equation:

$$B = \frac{0,125}{A^{0,41}} \quad (6)$$

The correlation coefficient is  $r = 0,86$ , implying good correlation. The compression curve can now be described exactly by these A and B parameters.

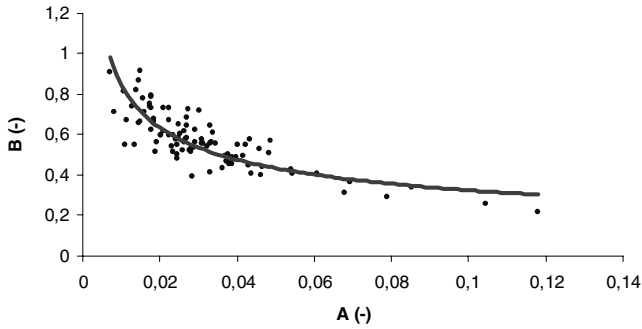


Figure 4. A and B parameters from oedometer test results

Further investigations were performed to establish correlations for other parameters. The relationship between parameter A and water content gives the best result (figure 5). The correlation coefficient is only  $r=0,64$ , which means moderately close relationship. The equation of the line is

$$A = \frac{3 \cdot w - 35}{1000} \quad (7)$$

The relation of the oedometer modulus due to primary compression and the modulus due to unloading/reloading is shown on figure 6. The second modulus is 3,6 times bigger than the first modulus with a correlation coefficient  $r = 0,7$ .

Figure 7. shows the correlation between the stress dependent stiffness according to a power law ( $m = 1-B$ ) and the consistency index. It can be seen that the average m parameter hardly changes with the consistency index. The average value is  $m = 0,45$  in case of plastic and hard clay.

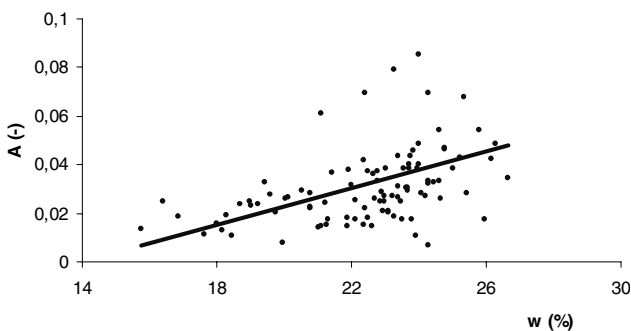


Figure 5. Relation between parameter A and water content

#### 4 SUMMARY

In order to produce the software input parameters, for more complicated soil models, more demanding laboratory tests are

needed. The basic demands are to determine the power for stress-level dependency of stiffness (m), tangent stiffness for primary oedometer loading ( $E_{oed}^{ref}$ ) and unloading/reloading stiffness ( $E_{ur}^{ref}$ ) when using the Hardening Model.

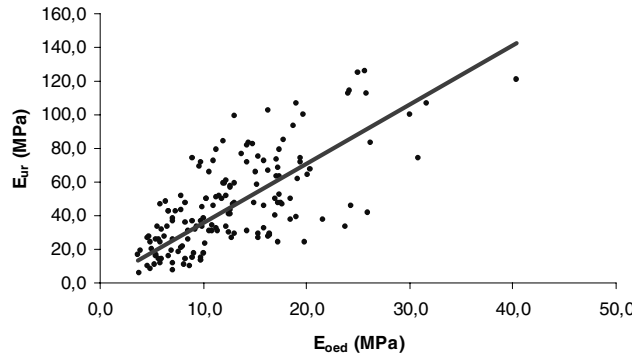


Figure 6. Relation between  $E_{oed}$  and  $E_u$

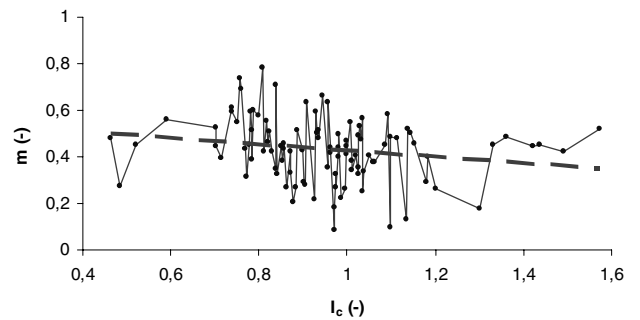


Figure 7. Relation between m and consistency index,  $I_c$

The correlations determined from over 200 oedometer and index tests are:  $A = (3 \cdot w - 35) / 1000$ ,  $B = 0,125 / A^{0,41}$ ,  $E_{ur} = E_{oed} \cdot 3,6$ ,  $m = 0,45$ .

These parameters are in agreement with the recommended value in the Plaxis manual. They can be applied by geotechnical engineers in cases where only index properties are available or when they are performing preliminary evaluations. These correlations also add confidence to the analyst when performing computations using Plaxis or other sophisticated programs.

#### ACKNOWLEDGEMENTS

This project has been undertaken by the Department of Structural Engineering, Széchenyi István University, Hungary.

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