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Geophysical properties of soils

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ABSTRACT: Low energy perturbations used in geophysical methods provide insightful information about constant-fabric soil properties and their spatial variability. There are causal links between soil type, index properties, elastic wave velocity, electromagnetic wave parameters and thermal properties. Soil type relates to the stress-dependent S-wave velocity, thermal and electrical conductivity and permittivity. The small strain stiffness reflects the state of stress, the extent of diagenetic cementation and/or freezing. Pore fluid chemistry, fluid phase and changes in either fluid chemistry or phase manifest through electromagnetic measurements. The volumetric water content measured with electromagnetic techniques is the best predictor of porosity if the water saturation is 100%. Changes in water saturation alter the P-wave velocity when $S_r \rightarrow 100\%$, the S-wave velocity at intermediate saturations, and the thermal conductivity when the saturation is low $S_r \rightarrow 0\%$. Finally, tabulated values suffice to estimate heat capacity and latent heat for engineering design, however thermal conductivity requires measurements under proper field conditions.

1 INTRODUCTION

Geophysical methods have played a crucial role in subsurface characterization, in the detection of hydrocarbon and mineral resources, and in monitoring a wide range of subsurface processes. Geophysical surveys are minimally invasive and involve low-energy stimuli, thus, they are inherently non-destructive constant-fabric measurements. In addition, the same geophysical assessment takes place in laboratory studies as in field surveys (Note: laboratory measurements may require careful analysis prior to the interpretation of field data due to frequency-dependent wave dispersion and scattering).

Geophysical parameters are most relevant to engineering design. This manuscript presents a concise yet practical summary of the geophysical properties of soils. The four central themes include: soil classification, characterization with elastic waves, characterization with electromagnetic waves and thermal properties.

2 SOIL CLASSIFICATION

Step 1: Coarse or fine? Let's accept the general definition of gravel (retained on sieve #4), sand (passing through sieve #4 and retained on sieve #200) and fines (passing through sieve #200). Any one of these soil components can control the mechanical and hydraulic behaviour of a soil mixture. For example, a densely packed sand near e_s^{min} will carry the load and

control the mechanical behaviour of a sand-gravel mixture when the gravel is looser than e_G^{max} . Similar analyses define the 13 notable mixtures listed in Table 1. The gravimetric-volume equations presented in this table compute the corresponding fractions for gravel, sand and fines. Specific factors included in the definition of these mixtures reflect an extensive database of soil properties (details in Park & Santamarina 2016). These notable mixtures determine classification boundaries in the triangular RSCS classification chart. Analyses and experimental data demonstrate that mixture thresholds are different for flow and mechanical control. Table 1 presents the classification procedure:

- Input the coefficient of uniformity C_u and the mean particle roundness R , of gravel and sand fractions (or their values of e^{max} and e^{min}).
- Input the liquid limit LL of fines (or the void ratio of fines at $\sigma' = 10$ kPa, $\sigma' = 1$ MPa, and at the liquid limit LL).
- Compute notable mixtures ①-through-⑨ for mechanical-control and ⑩-through-⑬ for flow control; plot the 13 notable mixtures on the triangular chart and draw the classification boundaries. Note: the Excel file available on the authors' websites simultaneously draws the chart, classification boundaries and plots the point that represents the soil under consideration.
- Classify the soil under consideration. The double letter nomenclature recognizes: first, the soil fraction that controls the mechanical behaviour and second, the soil fraction that controls flow (in parenthesis).

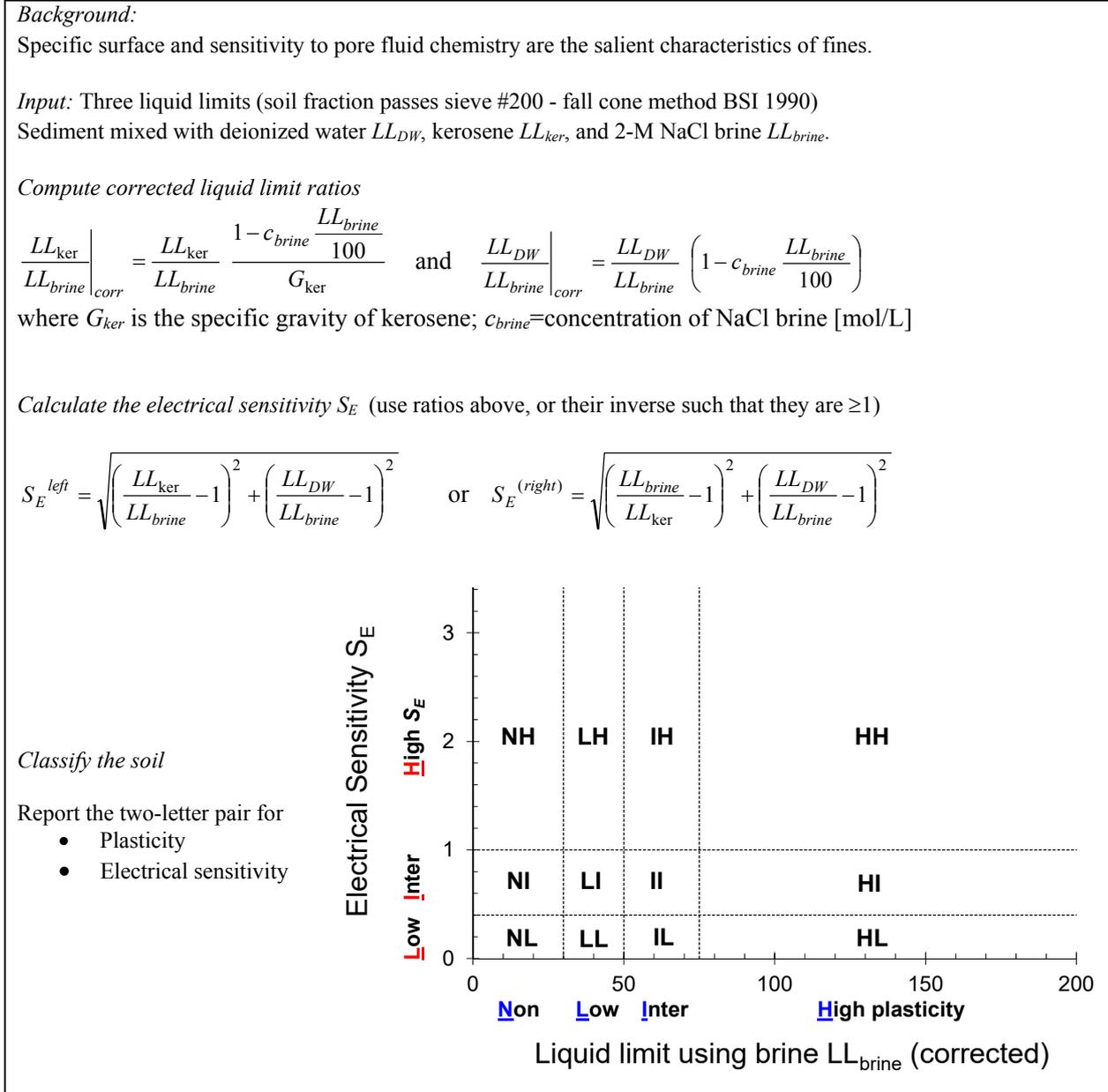
Table 1. Revised Soil Classification System RSCS.

Background:																																																																
Physics-based: gravimetric-volumetric analysis																																																																
Data-driven: takes into consideration extensive databases of soil behaviour																																																																
Input:																																																																
Gravel $G (> 4.75\text{mm})$	F_G	e_G^{\max} and e_G^{\min}	or roundness R and uniformity C_u																																																													
Sand $S (0.075\sim 4.75\text{mm})$	F_S	e_S^{\max} and e_S^{\min}	or roundness R and uniformity C_u																																																													
Fines $F (< 0.075\text{mm})$	F_F	$e_F ^{10\text{kPa}}$, $e_F ^{1\text{MPa}}$, and $e_F ^{LL}$	or liquid limit LL																																																													
Compute Threshold Fractions																																																																
Gravel fraction $F_G=M_G/M_T$		Sand fraction $F_S=M_S/M_T$																																																														
$F_G = \left(1 + \frac{e_G}{1+e_S} + \frac{e_S}{1+e_F} \frac{e_G}{1+e_S} \right)^{-1}$		$F_S = \left(\frac{1+e_S}{e_G} + 1 + \frac{e_S}{1+e_F} \right)^{-1}$																																																														
		$F_F = \left(\frac{1+e_S}{e_G} \frac{1+e_F}{e_S} + \frac{1+e_F}{e_S} + 1 \right)^{-1}$																																																														
Support information & Correlations:																																																																
Fines: Fluid flow $e_F ^{flow} = 0.05LL \log(LL - 25)$																																																																
Fines: Load carrying $e_F ^{10\text{kPa}} = e_F ^{1\text{kPa}} - C_c = 0.026LL + 0.07$		$e_F ^{1\text{MPa}} = e_F ^{1\text{kPa}} - 3C_c = 0.011LL + 0.21$																																																														
Gravel and sand: $e_C^{\max} = 0.032 + \frac{0.154}{R} + \frac{0.522}{C_u}$,		$e_C^{\min} = -0.012 + \frac{0.082}{R} + \frac{0.371}{C_u}$																																																														
<table border="1"> <thead> <tr> <th rowspan="2">No.</th> <th colspan="3">Notable Mixtures</th> </tr> <tr> <th>Gravel</th> <th>Sand</th> <th>Fines</th> </tr> </thead> <tbody> <tr> <td rowspan="9">(a) Load carrying</td> <td>①</td> <td>e_G^{\min}</td> <td>-</td> <td>$e_F ^{10\text{kPa}}$</td> </tr> <tr> <td>②</td> <td>e_G^{\min}</td> <td>e_S^{\max}</td> <td>-</td> </tr> <tr> <td>③</td> <td>e_G^{\min}</td> <td>e_S^{\max}</td> <td>$e_F ^{10\text{kPa}}$</td> </tr> <tr> <td>④</td> <td>-</td> <td>e_S^{\min}</td> <td>$e_F ^{10\text{kPa}}$</td> </tr> <tr> <td>⑤</td> <td>$2.5e_G^{\max}$</td> <td>e_S^{\min}</td> <td>-</td> </tr> <tr> <td>⑥</td> <td>$2.5e_G^{\max}$</td> <td>e_S^{\min}</td> <td>$e_F ^{10\text{kPa}}$</td> </tr> <tr> <td>⑦</td> <td>$1.3e_G^{\max}$</td> <td>-</td> <td>$e_F ^{1\text{MPa}}$</td> </tr> <tr> <td>⑧</td> <td>-</td> <td>$1.3e_S^{\max}$</td> <td>$e_F ^{1\text{MPa}}$</td> </tr> <tr> <td>⑨</td> <td>$2.5e_G^{\max}$</td> <td>$1.3e_S^{\max}$</td> <td>$e_F ^{1\text{MPa}}$</td> </tr> <tr> <td rowspan="4">(b) Flow</td> <td>⑩</td> <td>e_G^{\min}</td> <td>-</td> <td>$\lambda e_F ^{LL}$</td> </tr> <tr> <td>⑪</td> <td>e_G^{\min}</td> <td>e_S^{\max}</td> <td>$\lambda e_F ^{LL}$</td> </tr> <tr> <td>⑫</td> <td>$2.5e_G^{\max}$</td> <td>e_S^{\min}</td> <td>$\lambda e_F ^{LL}$</td> </tr> <tr> <td>⑬</td> <td>-</td> <td>e_S^{\min}</td> <td>$\lambda e_F ^{LL}$</td> </tr> </tbody> </table>				No.	Notable Mixtures			Gravel	Sand	Fines	(a) Load carrying	①	e_G^{\min}	-	$e_F ^{10\text{kPa}}$	②	e_G^{\min}	e_S^{\max}	-	③	e_G^{\min}	e_S^{\max}	$e_F ^{10\text{kPa}}$	④	-	e_S^{\min}	$e_F ^{10\text{kPa}}$	⑤	$2.5e_G^{\max}$	e_S^{\min}	-	⑥	$2.5e_G^{\max}$	e_S^{\min}	$e_F ^{10\text{kPa}}$	⑦	$1.3e_G^{\max}$	-	$e_F ^{1\text{MPa}}$	⑧	-	$1.3e_S^{\max}$	$e_F ^{1\text{MPa}}$	⑨	$2.5e_G^{\max}$	$1.3e_S^{\max}$	$e_F ^{1\text{MPa}}$	(b) Flow	⑩	e_G^{\min}	-	$\lambda e_F ^{LL}$	⑪	e_G^{\min}	e_S^{\max}	$\lambda e_F ^{LL}$	⑫	$2.5e_G^{\max}$	e_S^{\min}	$\lambda e_F ^{LL}$	⑬	-	e_S^{\min}	$\lambda e_F ^{LL}$
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Classify the soil. Report the two-name nomenclature: first letter/letters indicate the load-carrying fraction the second letter indicates the flow-controlling fraction. If either letter is $F \rightarrow$ proceed to classify the fines - Table 2.																																																																
Sources: Park and Santamarina (2016).																																																																

Step 2: Fines classification. Soils that are fines-controlled -either in their mechanical and/or flow response- require further analysis to determine that type of fines. The most salient characteristics of fines are (1) their specific surface, assessed by the liquid limit, and (2) their sensitivity to pore fluid chemistry. We determine fluid sensitivity by running liquid limits with deionized water LL_{DW} , brine LL_{brine} to collapse the double layer (2 M NaCl solution), and kerosene LL_{ker} to explore the effect of van der Waals forces.

Measured liquid limits are corrected for specific gravity and precipitated salts. Then two ratios LL_{ker}/LL_{brine} and LL_{DW}/LL_{brine} combine the corrected values as demonstrated in Table 2. The electrical sensitivity S_E captures the distance between measured values and the absolute “non-sensitive” soil response at $LL_{ker}/LL_{brine}=1$ and $LL_{DW}/LL_{brine}=1$. The two-letter pair classification of a fine soil recognizes its plasticity and its electrical sensitivity (Table 2).

Table 2. Fines Classification based on Plasticity and Sensitivity to Pore-Fluid Chemistry.



Sources: Jang and Santamarina (2016a); Jang and Santamarina (2016b)

3 ELASTIC WAVES

A small-strain mechanical perturbation propagates through the soil mass as an elastic wave. The wave equation for mechanical wave propagation combines Newton's law $F=m \cdot a=m \cdot d^2u/dt^2$, dynamic force equilibrium, constitutive equations (Hooke's law $\sigma=E\varepsilon$), and compatibility of deformations. The resulting wave equation anticipates two modes of propagation in a linear-elastic, homogeneous, isotropic, single-phase and infinite continuum: (1) S-waves where the particle motion is normal to the direction of propagation, and (2) P-waves where the particle motion is in the direction of wave propagation. New forms of wave propagation emerge anytime the above assumptions are relaxed, for example: shock waves (large

strain); reflection, refraction and scatter (heterogeneous); S-wave splitting (anisotropy); slow & fast waves (mixed phase); Rayleigh, Love, and tube waves (bounded media).

Wave velocity The shear stiffness of the granular skeleton G_{sk} defines the S-wave velocity V_s . Therefore, V_s increases with effective stress, diagenesis (e.g., cementation, creep, and salt precipitation), and suction (Table 3).

The P-wave velocity V_p depends on the constrained modulus of the soil M_{soil} , which is a function of the shear stiffness of the skeleton G_{sk} (see above) and the bulk stiffness of the soil B_{soil} . The bulk stiffness of the soil can be computed by successive substitutions to capture (Table 3): the skeleton stiffness B_{sk} and porosity n , the stiffness of water and air B_w and B_a , and the degree of saturation S_r as presented in Table 3.

V_P/V_S - Poisson's ratio. Theory of elasticity anticipates that the ratio V_P/V_S is a function of Poisson's ratio ν (Table 3). For small-strain wave propagation, Poisson's ratio is $\nu=0.15\pm 0.05$ for dry or unsaturated soils, but it tends to $\nu\rightarrow 0.5$ for well saturated soils; for example, Poisson's ratio can be $\nu=0.485$ for a saturated sand 20m deep and exceed $\nu=0.499$ for a saturated soft clay.

Attenuation. The wave amplitude decreases with distance due to (Table 4): geometric spreading of the propagating spherical or cylindrical front (i.e., same energy across a larger area), reflection and backscatter at interfaces (lower transmitted energy), and unrecovered energy consumed while deforming the material as the wave propagates (viscous, thermoelastic and/or frictional losses). Geometric spreading vanishes in plane waves.

Table 3. Elastic Waves: Velocity.

<i>S-wave</i> V_S		
saturated or dry soils; uncemented	$V_S = \sqrt{\frac{G_{sk}}{\rho}} = \alpha \left(\frac{\sigma'_{mean}}{1kPa} \right)^\beta$	where $\beta = 0.73 - 0.27 \log\left(\frac{\alpha}{m/s}\right)$
	σ'_{mean} mean effective stress on the polarization plane	
unsaturated soils	$V_S \approx V_{S(for S_r=1.0)} \left[1 + \frac{suction \cdot S_r}{0.75 \sigma'_v} \right]^\beta$	
<i>P-wave</i> V_P	$V_P = \sqrt{\frac{M_{soil}}{\rho_{soil}}} = \sqrt{\frac{B_{soil} + 4/3G_{sk}}{\rho_{soil}}}$	water $V_P=1482$ m/s air $V_P= 343$ m/s
<i>Bulk modulus and mass density</i> (Assumes $B_{sk}/B_g \approx 0$ and low frequency limit)		
Skeleton	$B_{sk} = \frac{2(1+\nu)}{3(1-2\nu)} G_{sk}$	G_{sk} from $G_{sk} = V_S^2 \rho$
Soil (fluid + skeleton)	$B_{soil} = B_{sus} + B_{sk}$	$\rho_{soil} = \rho_{sus} = (1-n)\rho_g + n\rho_{fl}$
Suspension (fluid + particles)	$B_{sus} = \left(\frac{1-n}{B_g} + \frac{n}{B_{fl}} \right)^{-1}$	$\rho_{sus} = (1-n)\rho_g + n\rho_{fl}$
Fluid Mixture	$B_{fl} = \left(\frac{S_r}{B_w} + \frac{1-S_r}{B_a} \right)^{-1}$	$\rho_{fl} = (1-S_r)\rho_a + S_r\rho_w$ $\rho_{fl} = S_r\rho_w$ in case $a=air$
V_P/V_S - Poisson's ratio	$\frac{V_P}{V_S} = \sqrt{\frac{M_{soil}}{G_{sk}}} = \sqrt{\frac{2(1-\nu)}{(1-2\nu)}}$	unsaturated soils $\nu=0.15\pm 0.05$ well saturated soils $\nu\rightarrow 0.5$

Sources: Richart *et al.* (1970); Hardin and Drnevich (1972); Reynolds (1997); Santamarina *et al.* (2001); Cho and Santamarina (2001). Based on an earlier compendium by Santamarina *et al.* 2005.

4 ELECTROMAGNETIC WAVES

An electrical or magnetic transient propagates through the soil mass as an electromagnetic wave. The wave equation for electromagnetic waves results from Maxwell's equations. The electrical field and the magnetic field oscillate transversely to the direction of propagation and to each other.

There are three electromagnetic material parameters: magnetic permeability μ , electrical conductivity σ_{el} , permittivity κ . Permittivity and permeability are complex quantities because they represent both in-and-out of phase responses. The three material pa-

rameters combine to determine the propagation velocity V and the material attenuation coefficient α or skin depth $S_d = 1/\alpha$ i.e., is the distance travelled by a plane wave when its amplitude decreases to $1/e$ of the initial amplitude. Table 5 summarizes equations for wave velocity and skin depth. Typically, most fluids and solids in the subsurface are either paramagnetic or diamagnetic; then, velocity and skin depth equations become those listed in the second half of Table 5.

Magnetization and polarization losses add to Ohmic conduction to render an effective conductivity. When the effective conductivity is high, the first term of the wave equation prevails and the electromagnetic transient propagates in diffusional mode.

Table 4. Elastic Waves: Attenuation

1 *Attenuation* $\frac{A_2}{A_1} = \left(\frac{r_1}{r_2}\right)^\zeta T e^{-\alpha(r_2-r_1)}$

2 Ratio between the amplitude of particle motion A at radial distances r_1 and r_2 [m]

3 Transmission coefficient T across an interface: a function of relative impedance

4 Exponent: plane wave $\zeta=0$; cylindrical front $\zeta=0.5$; spherical front $\zeta=1$

5 Relationship between linear attenuation coefficient α [1/m], skin depth S_d [m], and damping ratio D :

6 $\alpha = \frac{1}{S_d} = \frac{2\pi D}{\lambda}$ Note: the skin depth in terms of wavelengths is $\frac{S_d}{\lambda} = \frac{1}{2\pi D}$

7 *Physical processes in material attenuation*

Dry - small strain: thermo-elastic relaxation

Moist/wet - small strain: viscous loss prevails

Large strain: frictional loss

Typical damping values at small strain for P- and S- waves

<u>Material</u>		<u>Damping D</u>	<u>Comments</u>
Air		2×10^{-4}	Changes with relative humidity
Water		2×10^{-6}	Increases with dissolved gas
Coarse soils	<i>dry</i>	0.002~0.008	Increases when wet
	<i>saturated</i>	0.005~0.02	
Fine soils	<i>saturated</i>	0.01~0.05	
Organic soils	<i>saturated</i>	0.01~0.05	
Rocks	<i>dry</i>	0.002~0.004	
	<i>wet</i>	0.006~0.025	

Notes: γ is the strain, σ_0' is the effective confinement, w_g is the gravimetric water content. Sources: Johnston and Toksoz 1980; Yasuda and Matsumoto (1993); Kim *et al.* (1991); Laird and Stokoe (1993); Santamarina and Cascante (1996); Li *et al.* (1998); Kokusho (1980); Kokusho *et al.* (1982); Cascante and Santamarina (1996); Diaz-Rodriguez and Santamarina (2001); Kim and Novak (1981).

Table 5. Electromagnetic Waves: Velocity and Attenuation.

Electromagnetic wave propagation

Maxwell's Equations $\frac{\partial^2 E}{\partial x^2} = \mu\sigma \frac{\partial E}{\partial t} + \mu\epsilon \frac{\partial^2 E}{\partial t^2}$

Electromagnetic properties

Permeability	μ^*	Relative $\mu_r = \mu^*/\mu_0$	free space $\mu_0 = 4\pi \cdot 10^{-7}$ H/m
Permittivity	ϵ^*	Relative $\kappa = \epsilon^*/\epsilon_0$	free space $\epsilon_0 = 8.85 \times 10^{-12}$ C ² N ⁻¹ m ⁻²
Conductivity	σ_{el}		

Velocity (non-ferromagnetic)

$$V = c_0 \frac{1}{\sqrt{\frac{1}{2} \left[\sqrt{\kappa^2 + \left(\frac{\sigma}{\epsilon_0 \omega}\right)^2} + \kappa \right]}}$$

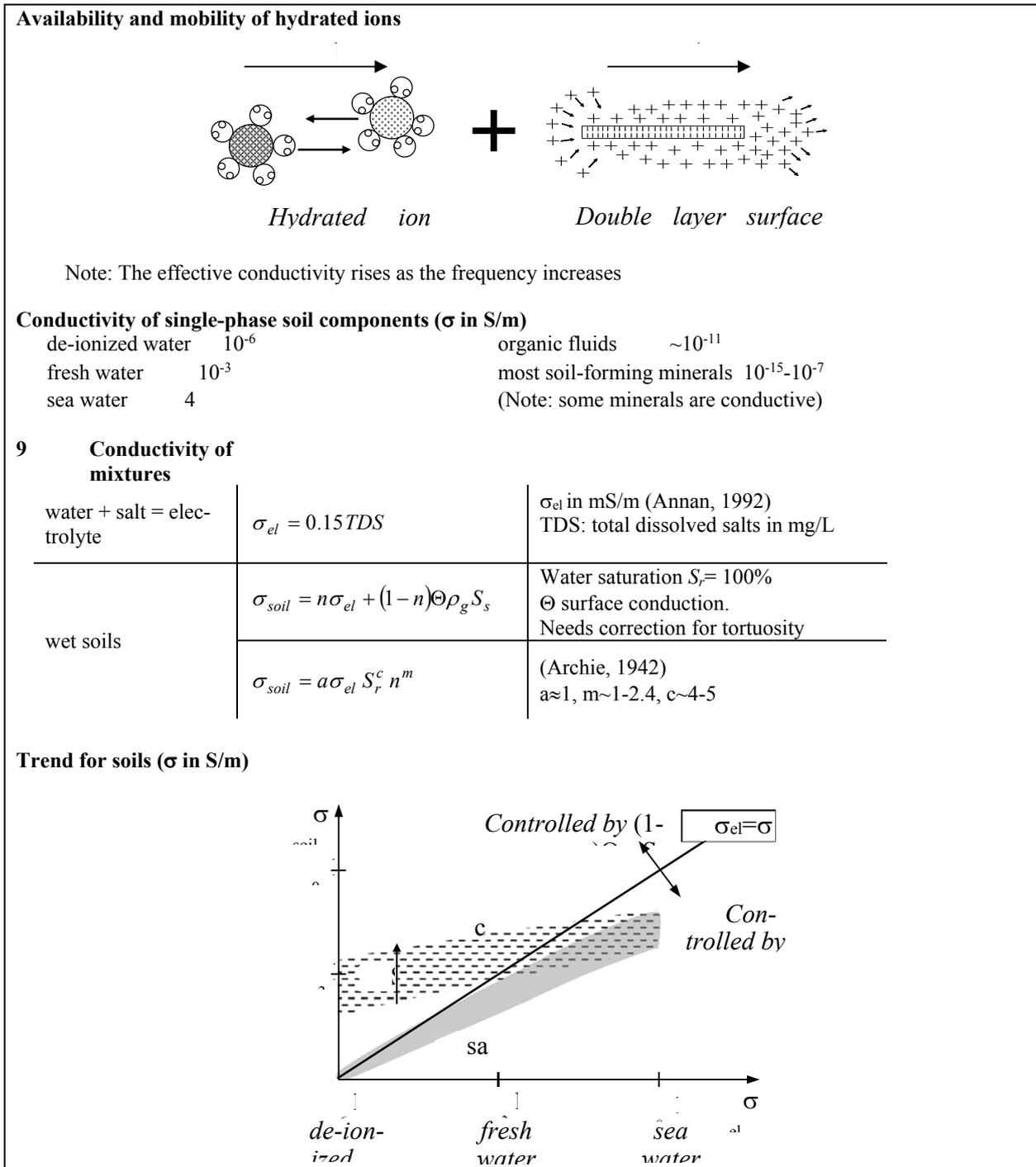
In free space $c_0 = 1/\sqrt{\epsilon_0 \mu_0} = 3 \times 10^8$ m/s

Attenuation (non-ferromagnetic)

Linear attenuation $\alpha = 1/S_d$

$$S_d = \frac{c_0}{\omega} \frac{1}{\sqrt{\frac{1}{2} \left[\sqrt{\kappa^2 + \left(\frac{\sigma}{\epsilon_0 \omega}\right)^2} - \kappa \right]}}$$

Table 6. Electrical Conductivity.



Notes: The surface conduction for kaolinite is about $\Theta \approx 10^{-9}$ Siemens. Tortuosity may reduce the electrical conductivity in clays more than in sands. Hence, the conductivity of marine clays may be lower than the conductivity of marine sands, at the same void ratio.

Sources: Annan (1992); Reynolds (1997); Santamarina *et al.* (2001). Based on an earlier compendium by Santamarina *et al.* (2005).

Electrical conductivity. The movement of hydrated ions is responsible for electrical conduction in geomaterials. Hydrated ions imply the presence of water, dissolved salts (both cations and anions), and hydrated counter-ions next to charged mineral surfaces (diffuse double layer). Therefore, the electrical conductivity of soils is proportional to the volumetric water content, the conductivity of the pore fluid which increases linearly with salt concentration c (for low $c < \sim 0.2M$), and the specific surface of the soil; Table

6 lists convenient semi-empirical models. Pore fluid conductivity prevails in sands and silts, while surface conduction gains relevance in low porosity, high specific surface clayey sediments saturated with low salt concentration water (Table 6).

Permittivity. Permittivity is a measure of polarizability. Free water molecules control the permittivity of soils and rocks in the MHz-to-GHz frequency range; therefore, the permittivity of wet soils is proportional to the volumetric water content $\theta_v = S_r n$. By

contrast, the orientational polarization of water is hindered when water is frozen, in adsorbed layers close to mineral surfaces and when water molecules hydrate ions. Table 7 summarizes semi-empirical models.

Permeability. We can assume that soils are non-ferromagnetic in the absence of ferromagnetic inclusions. Otherwise, the volume fraction of ferromagnetic inclusions determines the magnetic permeability of the soil (Table 8).

Table 7. Permittivity (Relevant frequency range 1 MHz-1 GHz).

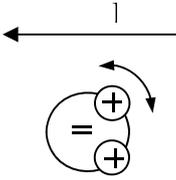
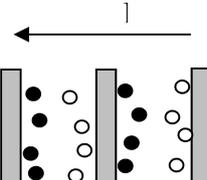
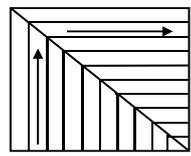
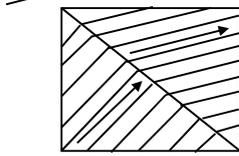
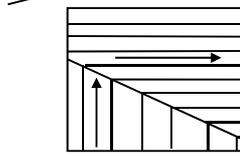
Polarization			
	+		
<i>orientation of polar molecules</i>		<i>interfacial polarization</i>	
Note: Permittivity increases as frequency decreases			
Permittivity of single-phase soil components (radio frequencies)			
water	78.5	quartz	4.2 - 5
methanol	32.6	calcite	7.7 - 8.5
most organic fluids	2 - 6	most minerals	6 - 10
Permittivity of wet soils ($\theta_v = S_r \cdot n$)			
$\kappa' = 1.40 + 87.6 \theta_v - 18.7 \theta_v^2$	50 MHz	Wensink (1993)	
$\kappa' = 3.03 + 9.3 \theta_v + 146.0 \theta_v^2 - 76.7 \theta_v^3$	MHz to GHz	Topp et al. (1980)	
$\kappa' = 3.3 + 41.4 \theta_v + 16.0 \theta_v^2$	~ 1GHz	Wensink (1993)	
$\kappa' = 3.14 + 23.8 \theta_v + 16.0 \theta_v^2$		Wang (1980)	
$\kappa' = 40 \theta_v - 3.9 + \sqrt{44.8 - 392 \theta_v + 1600 \theta_v^2}$		Selig and Mansukhani (1975)	
$\kappa' = (2.6 - 1.6n + 7.9 \theta_v)^2$		Based on CRI mixture model	

Table 8: Magnetic Permeability.

Magnetization	
	(a)
	(b)
	(c)
Magnetization mechanisms in ferromagnetic materials: (a) no magnetic field $H=0$; (b) rotation of spins within domains $H>0$; and (c) translation of domain walls $H>0$.	
Single materials	
water, quartz, kaolinite	~0.9999 (diamagnetic)
montmorillonite, illite, granite, hematite	1.00002-1.0005 (paramagnetic)
nickel, iron	> 300 (ferromagnetic)
Predictive relations	
Wagner's model for spherical particles ⁽¹⁾	$\mu' = 1 + 3v_{Fe}$ for $v_{Fe} < 0.2$
Kaolinite with iron filings (at 10 kHz) ⁽²⁾	$\mu' = 1 + 4v_{Fe} + 7v_{Fe}^2$ for $v_{Fe} < 0.3$

Sources: (1) Göktürk *et al.* (1993); (2) Klein and Santamarina (2000)

Note: v_{Fe} is the volume fraction of ferromagnetic inclusions

5 THERMAL PROPERTIES

Table 9 schematically summarizes thermal conduction phenomena.

Table 9: Thermal Phenomena in Soils.

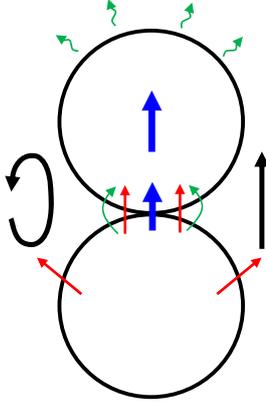
Parameters					
<i>Latent heat</i> L [kJ/kg]: Heat required for phase transformation at constant temperature.					
<i>Specific heat</i> c_p [$\text{Jkg}^{-1}\text{K}^{-1}$]: Heat required to increase the temperature of 1 kg by 1 K.					
<i>Thermal conductivity</i> k_T [$\text{Wm}^{-1}\text{K}^{-1}$]: relates the heat flux density q [$\text{J}/\text{sec}/\text{m}^2$] to the thermal gradient $q = k_T \Delta T / \Delta x$ (Fourier's heat law)					
<i>Thermal diffusivity</i> : $D_T = k_T / \rho c_p$.					
<i>Volumetric expansion coeff</i> α_T [K^{-1}]: Relates temperature change to strain $\varepsilon = \alpha \Delta T$					
Typical values					
Material	Latent heat [kJ/kg]	Specific heat c_p [$\text{Jkg}^{-1}\text{K}^{-1}$]	Thermal conduct. k_T [$\text{Wm}^{-1}\text{K}^{-1}$]	Thermal diffusivity D_T [$\text{m}^2\text{sec}^{-1} \times 10^{-7}$]	Volumetric thermal expansion coefficient α_T [10^{-6}K^{-1}]
Quartz (single crystal)		750	12 () - 6.8 (\perp)	45	800 ()-1400 (\perp)
Shale		630	1.56	31	
Limestone		900	1.3	27	3.3
Sand	dry	800	0.15 - 0.33		
	water sat	2200	2 - 4		
Water	334	4200	0.6	1.4	200 (at 293K)
Ice (0 °C)	334	2040	2.2	11.2	51 (at 273K)
Air		1000	0.024	0.21	3400 (at 293K)

Trends: General $k_{T, \text{dry soil}} < k_{T, \text{wet soil}} < k_{T, \text{mineral}}$

Dry soils $k_{T, \text{dry}} = \frac{0.135 \rho_{\text{dry}} + 64.7}{\rho_g - 0.947 \rho_{\text{dry}}}$ (Johansen 1975)

Wet soils $k_{T, \text{wet}} = k_{T, \text{dry}} + (1 - e^{-0.89 S_r})(k_{T, \text{sat}} - k_{T, \text{dry}})$ (Ewen and Thomas 1987)

Thermal conduction: Grain and pore-scale processes



Particle conduction
Contact conduction

Radiation
Particle-particle radiation

Particle-fluid conduction
Particle-fluid-part conduction

Pore fluid conduction
Pore fluid convection

k_T increase with:

- porosity $n \downarrow$
- effective stress $\sigma' \uparrow$ (heat transfer at contacts \uparrow)
- water content \uparrow
- quartz content \uparrow
- frozen water
- coarser grains

A change in temperature propagates as a diffusion front through the soil mass, facilitated by the thermal conductivity of the soil yet hindered by the heat consumed in changing the temperature of the soil mass. The propagating thermal front causes volume strains, and phase changes may take place (vapour \leftrightarrow liquid \leftrightarrow solid). Consequently, the thermal properties of soils include: thermal diffusivity D_T , thermal conductivity k_T , specific heat c_p , latent heat L , and volumetric thermal expansion coefficient α_T . Table 9 presents definitions and typical values.

In general, we can use tabulated values and gravimetric or volumetric averages to estimate thermal properties for engineering analyses, except for the thermal conductivity (and hence diffusivity). Thermal conduction depends on:

- The type of mineral: quartz exhibits particularly high thermal conductivity
- The coordination number between grains: denser soils exhibit higher k_T
- The quality of contacts: contact resistance decreases as stress increases (it follows a power

function that resembles Hertzian contact behaviour), and in cemented soils

- The presence of water: while the thermal conductivity of water is lower than that of most minerals, the presence of water at contacts has a pronounced effect on the thermal conduction across contacts and the conductivity of the soil.

6 CLOSING THOUGHTS: GEOPHYSICS AND ENGINEERING

The previous sections identify various causal links between geophysical properties, soil type, index properties and soil behaviour. Salient causal relations follow:

- Soil type: related to stress-dependent changes in the S-wave velocity, thermal conductivity, electrical conductivity and permittivity.
- Small strain shear stiffness (for deformation-based design): it is computed from S-wave velocity V_s measurements using cross-hole down-hole and surface wave methods. Shear stiffness and V_s reflect effective stress –including suction, extent of diagenetic cementation and/or freezing. Exercise caution when soils are unsaturated as variation in saturation levels will result in changes in the shear stiffness.
- Porosity: from the volumetric water content calculated with electromagnetic measurements using ground penetrating radar, electrical resistivity or time domain reflectometry. In addition, electromagnetic parameters can be used to detect time-varying water saturation, pore fluid chemistry, and fluid phase (e.g., freezing).
- Other geophysical parameters mirror time varying water saturation, including P-wave velocity when $S_r \rightarrow 100\%$, S-wave velocity for intermediate saturations, and thermal conductivity when $S_r \rightarrow 0\%$.
- Thermal properties are needed for the design of systems such as buried cable installations and thermal piles. Specific and latent heats are gravimetric or volumetric averages of tabulated values for the individual soil components. The thermal conductivity (and hence diffusivity) can be measured in the lab under proper field stress and moisture conditions.

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8 LIST OF SYMBOLS

α	attenuation coefficient
α_T	volumetric thermal expansion coefficient
α, β	fitting parameters in velocity-stress relation
Δ	energy loss/cycle
ε	strain
ε^*	complex permittivity
ε_0	permittivity of free space, $\varepsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/(\text{N}\cdot\text{m}^2) = 8.85 \times 10^{-12} \text{ F/m}$
γ	shear strain (γ_{elas} elastic threshold strain)
κ	relative permittivity
λ	wavelength
μ^*	magnetic permeability (subscript r: relative permeability)
μ_0	magnetic permeability of free space, $\mu_0 = 4\pi \times 10^{-7} \text{ H/m}$
ν	Poisson's ratio
θ_v	volumetric water content
Θ	surface conduction
ρ	mass density (fl: fluid; g: mineral that makes the grains; sus: suspension; dry: bulk dry)
ζ	exponent in geometric attenuation that depends on wave front
σ_{el}	electrical conductivity (el: electrolyte; fl: fluid)
σ	stress (σ' : effective stress; v: vertical; h: horizontal; mean: mean in polarization plane)
ω	angular frequency
A	amplitude
a, c, m	constants used in Archie's equation
B	bulk stiffness (sk: soil skeleton; g: mineral that makes grains; sus: suspension; fl: fluid)
C_c	compression index
C_u	coefficient of uniformity
c_{brine}	concentration of NaCl brine [mol/L]
c_o	speed of light in free space, $c_o = 3 \times 10^8 \text{ m/s}$
c_p	specific heat [$\text{Jkg}^{-1}\text{K}^{-1}$]
D	damping ratio
D_T	thermal diffusivity
E	electric field
E	Young's modulus
F	soil fraction (G: gravel; S: sand; F: fines)
e	void ratio (subscripts G and S denote the gravel and sand, respectively)
f	frequency (r: resonant frequency)
G	shear modulus (sk: soil skeleton)
G_{ker}	specific gravity of kerosene
H	magnetic field
k_T	thermal conductivity (sat: saturated)
L	latent heat
LL	liquid limit (ker: kerosene; DW: de-ionized water)
M	constraint modulus
n	porosity
R	roundness
r	distance from source
S_d	skin depth
S_E	electrical sensitivity
S_r	degree of saturation
S_s	specific surface
T	transmission coefficient
TDS	total dissolved salts in mg/L
V	wave velocity (ph: phase; P: P-wave; S: S-wave; R: Rayleigh wave)
v_{Fe}	volume fraction of ferromagnetic inclusions
w_g	gravimetric water content

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